

## Example: Regular Grammar<sub>JP</sub>

Enter a regular grammar that generates the following language L over the alphabet  $\Sigma = \{a, b\}$ :

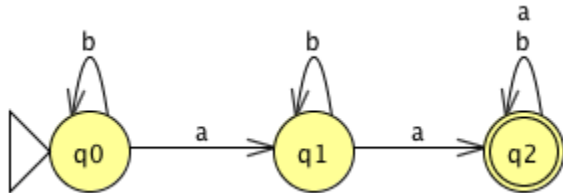
$$L = \{ w \mid w \text{ contains at least two } a \text{ symbols} \}$$

### Sample Solution (see RG\_XaXaX.jff)

Consider that the only constraint is two appearances of the symbol **a** and that any number of symbols may appear before and between them.

Recall that a regular grammar may be specified in right-linear format. Thus all productions must have at most one variable in the right-hand side and that variable must be consistently to the right of any terminals.

Note that one possible DFA for this language is the following (see DFA\_XaXaX.jff):



This suggests that the start symbol, in correspondence to state  $q_0$ , should be able to produce any number of **b** symbols followed by a string that contains the required number of **a** symbols.

$$S \rightarrow bS$$

Further, once an **a** is produced, the remaining string must simply contain at least one **a** symbol, corresponding to state  $q_1$ .

$$S \rightarrow aA$$

Similarly, the variable  $A$  should be able to produce any number of **b** symbols followed by a string that contains at least one **a** symbol.

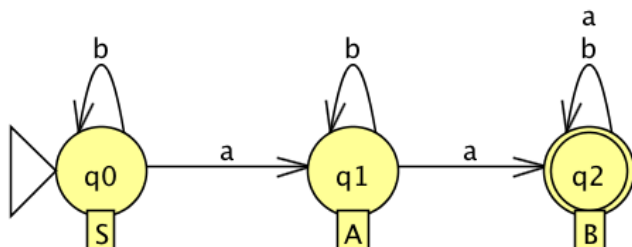
$$A \rightarrow bA$$

$$A \rightarrow aB$$

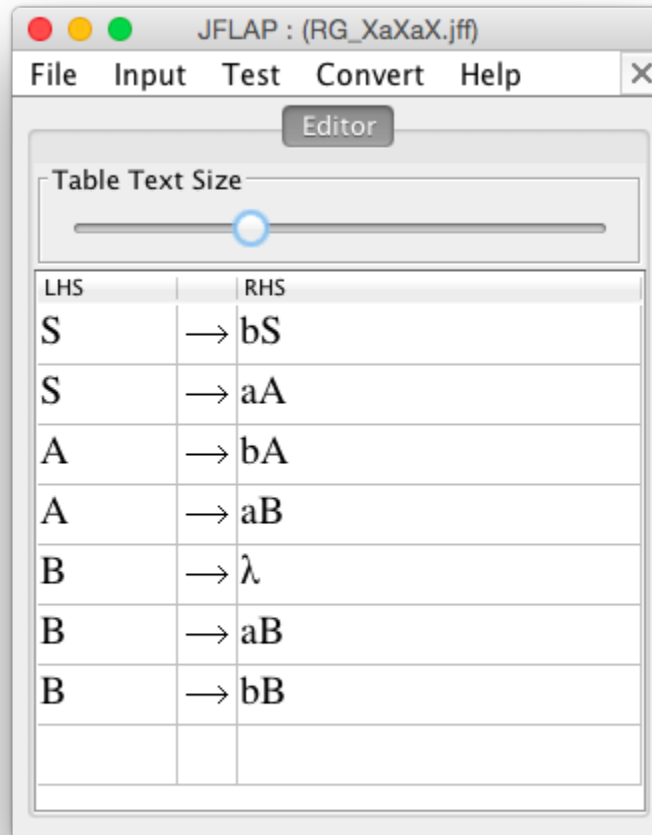
The remaining rules combine to produce all strings over  $\{a, b\}^*$ .

$$B \rightarrow \varepsilon \mid aB \mid bB$$

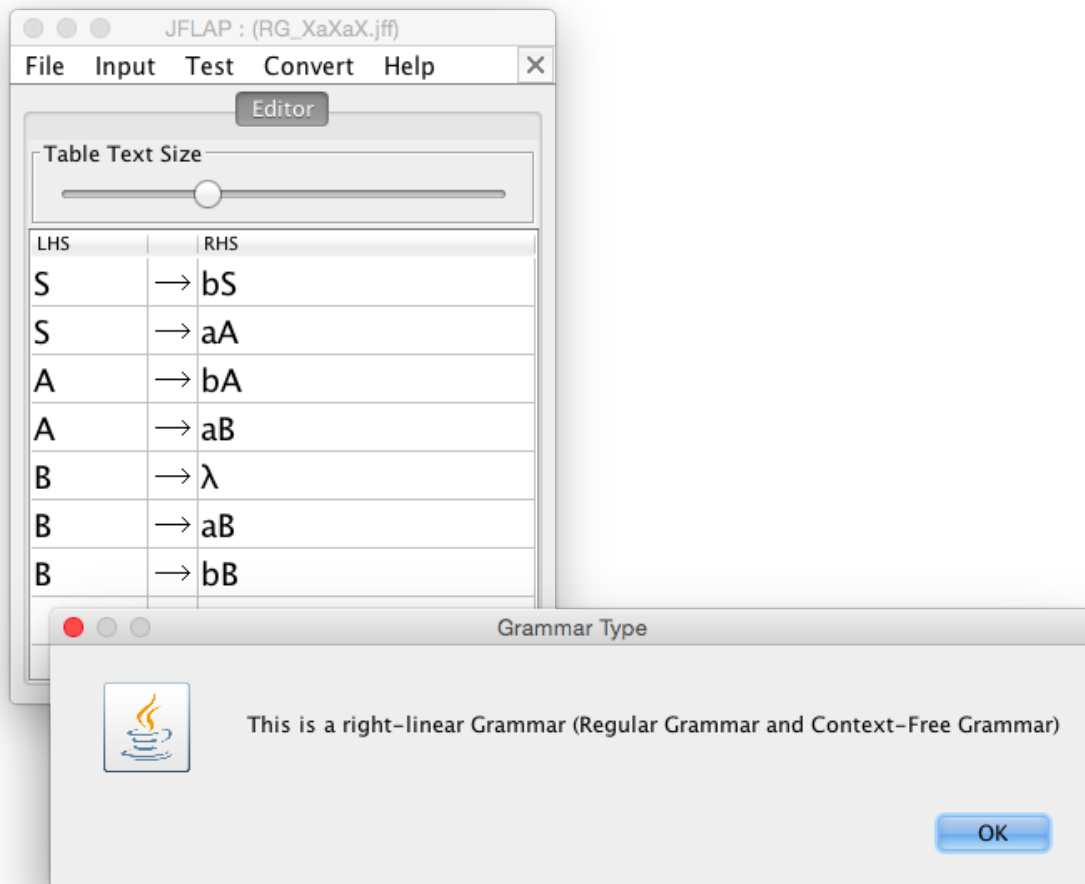
Here is the DFA with states annotated with the variables of this grammar.



1. Enter this grammar into JFLAP.



2. Check the type of grammar using *Test > Test for Grammar Type*.



3. Verify known strings using the *Brute Force Parse*.

JFLAP : (RG\_XaXaX.jff)

File Input Test Convert Help

Editor Brute Parser

Table Text Size

Start Pause Step Derivation Table

Input abba  
String accepted! 6 nodes generated.

LHS	RHS	Production	Derivation
S	→ bS	S→aA	S
S	→ aA	A→bA	aA
A	→ bA	A→bA	abA
A	→ aB	A→aB	abbaB
B	→ λ	B→λ	abba
B	→ aB		
B	→ bB		

Derived λ from B. Derivations complete.